

# From theory to real implementation in the NISQ era



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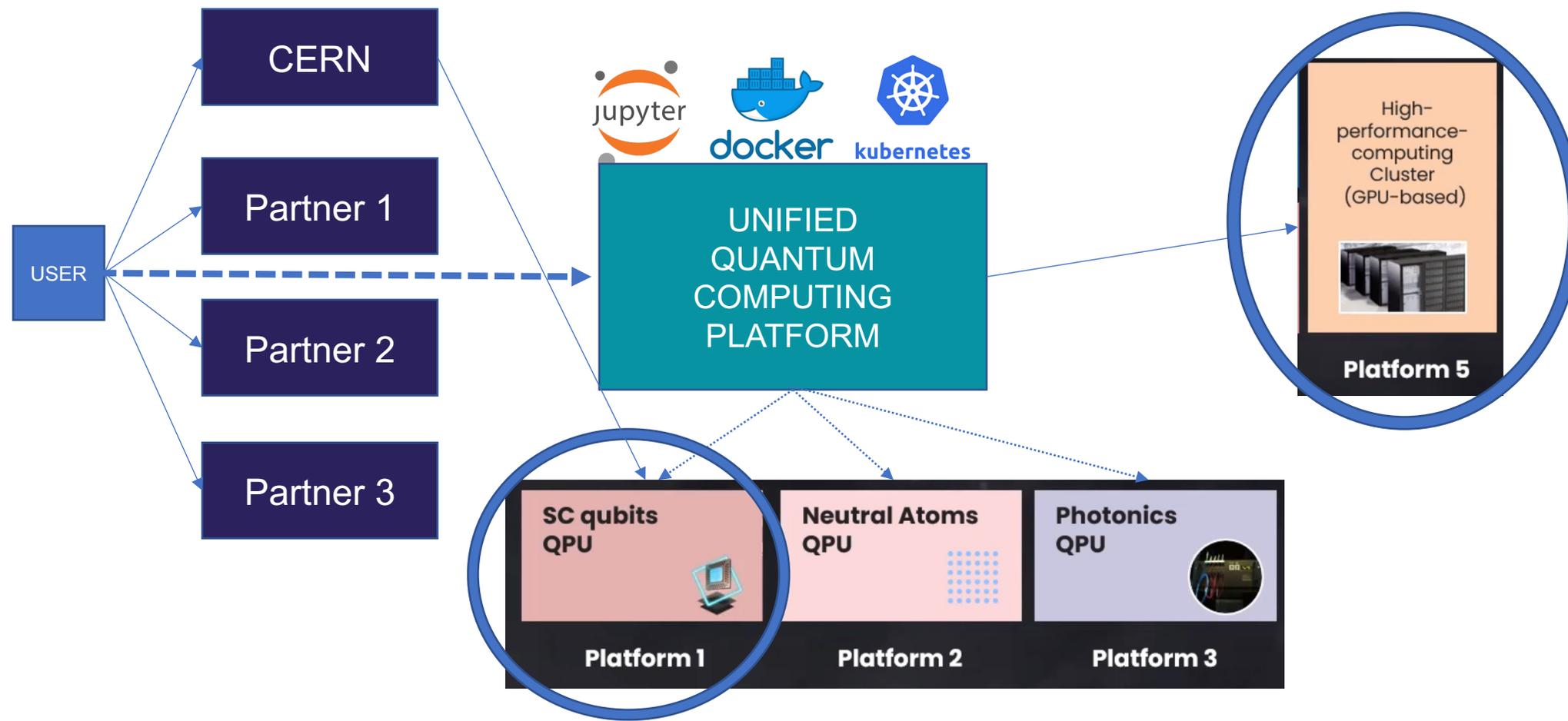
QUANTUM  
TECHNOLOGY  
INITIATIVE



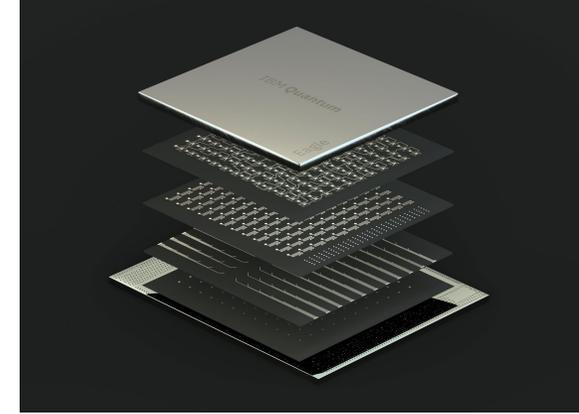
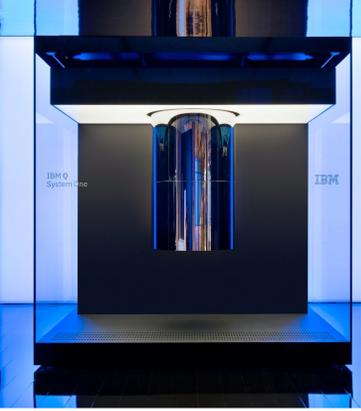
- **Quantum Computing and Simulation**
- **Some Examples**



# Quantum Computing Platform



# QUANTUM TECHNOLOGIES



## ***Near-term***

### ***Noisy Intermediate-Scale Quantum (NISQ) devices***

Available now, up to 433 qubits (IBM)

Smaller devices, typically noisier

Suffer from gate and other types of errors

Current algorithms are designed to deal with noise and errors: low-depth circuits

## ***Fault-tolerant***

Available (maybe) in the future

Many qubits, enabling complex computation

Error-free

Used for theoretical, high-depth algorithms

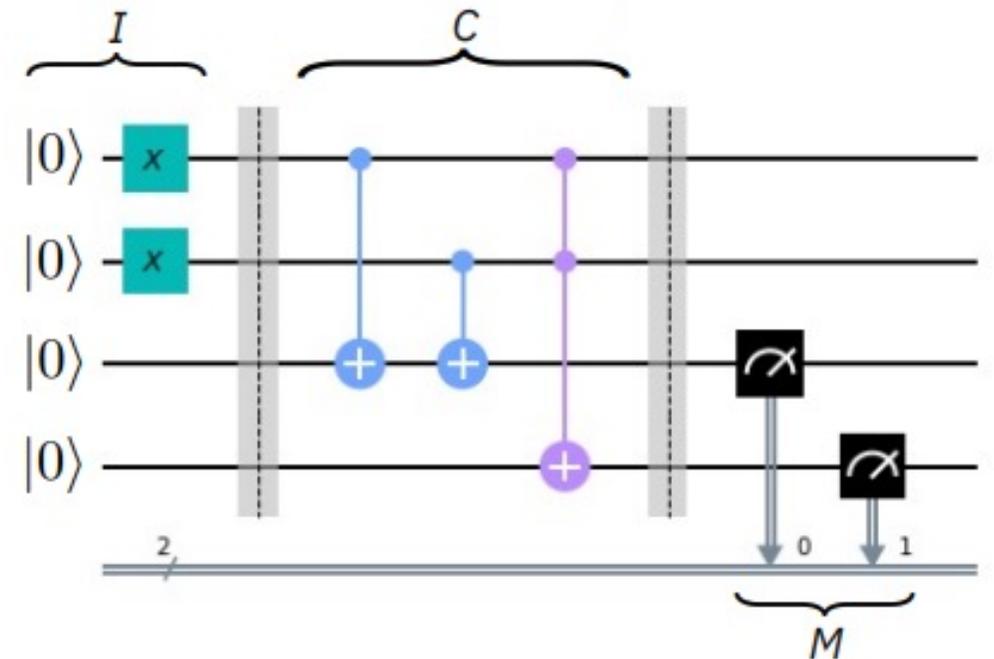
# Challenges of Quantum Programming

- Qubits are analog
- Quantum programs result in probabilistic outputs
- You can't read the entire exact state of a quantum program
- Each device (and qubit!) has characteristics a programmer has to be aware of, such as noise and connectivity
- Qubits have a short coherence time (or lifetime)

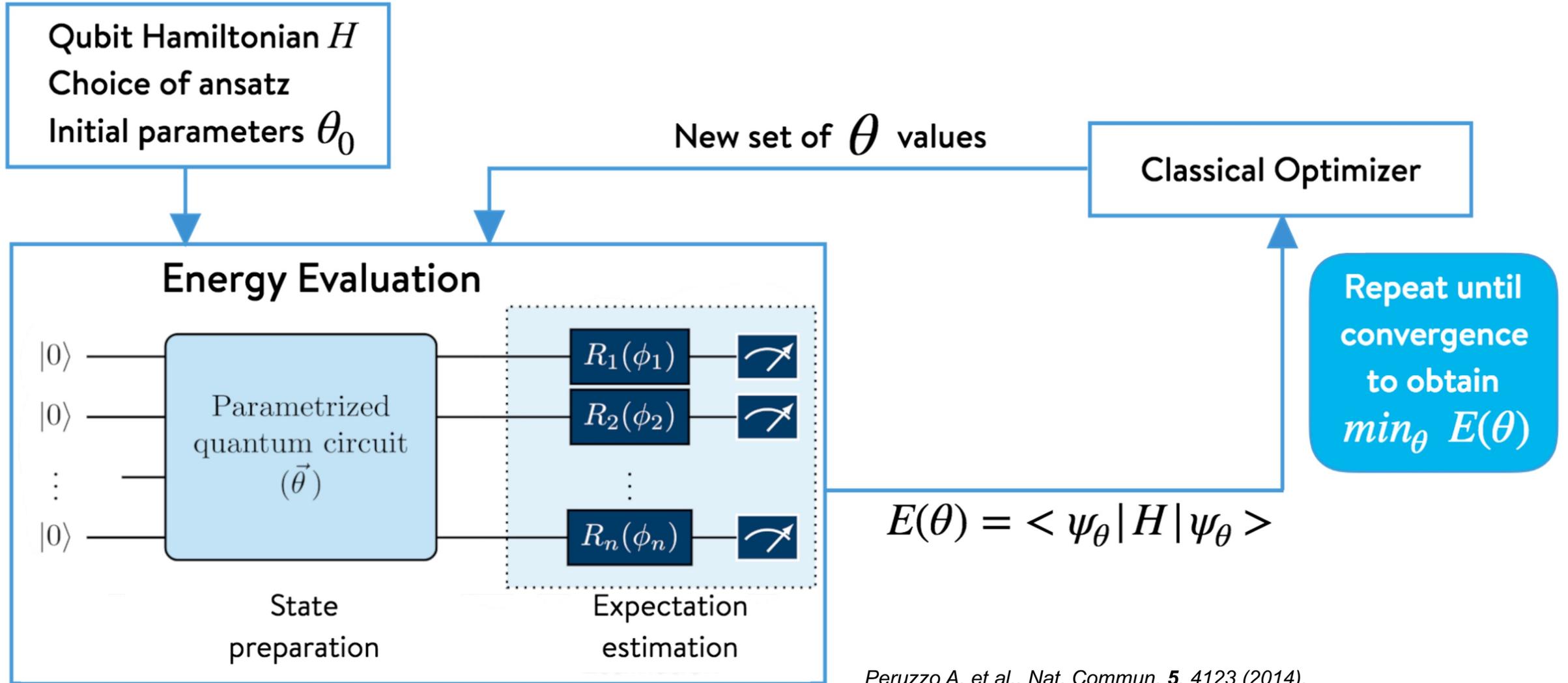
# Simulating a Quantum Computer

## Why and when to use simulator

- Prototype/understand quantum algorithms before running on a real device
- Simulation of large quantum systems is, in the general case, an exponentially hard computational task for a classical computer, *memory requirements double* for every qubit added
- *This in fact one of the main motivations for building a quantum computer in the first place!*
- For now, it's generally "cheaper" and "easier" to run an experiment, at least a small-scale one, on a simulator as compared to hardware
- In simulation we can understand noise properties of real devices and how noise affects performance (of e.g. algorithms)



# Going Hybrid: Variational Quantum Eigensolver (VQE)



Peruzzo A. et al., Nat. Commun. 5, 4123 (2014).



- Quantum Computing and Simulation
- **Some Examples**



# Finite-size criticality in the Lipkin-Meshkov-Glick (LMG) model

$$H = -\frac{1}{N} \sum_{i < j}^N \sigma_x^i \sigma_x^j + \gamma \sigma_y^i \sigma_y^j - B \sum_{i=1}^N \sigma_z^i.$$

System of  $N$  spins with **anisotropic interaction** in the  $x$ - $y$  plane, in an external **transverse magnetic field**.

- Study the finite size criticality (exponential number of degrees of freedom).
- Interpolation between fully connected Ising model and Lipkin-Dicke model.

Quantum phase transitions ( $N \rightarrow \infty$ ):  $E_{gs} = E_{1st}$   
Non-analyticity in the ground state energy (crossing)

*Grossi, Kiss et al, Finite-size criticality in fully connected spin models on superconducting quantum hardware - PhysRevE.107.024113*

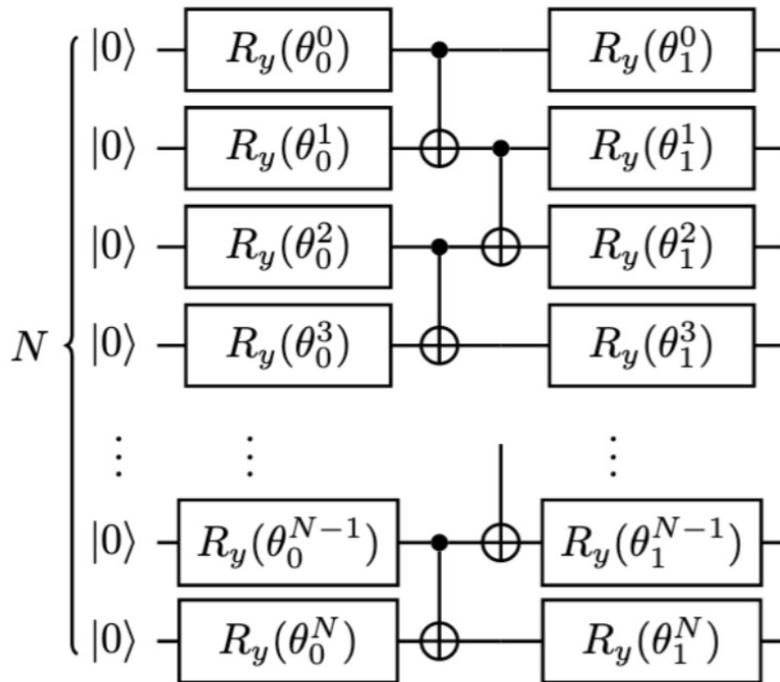
# VQE for excited states

Higgot et al, Quantum **3**, 156 (2019)

## Iterative eigenstates preparation

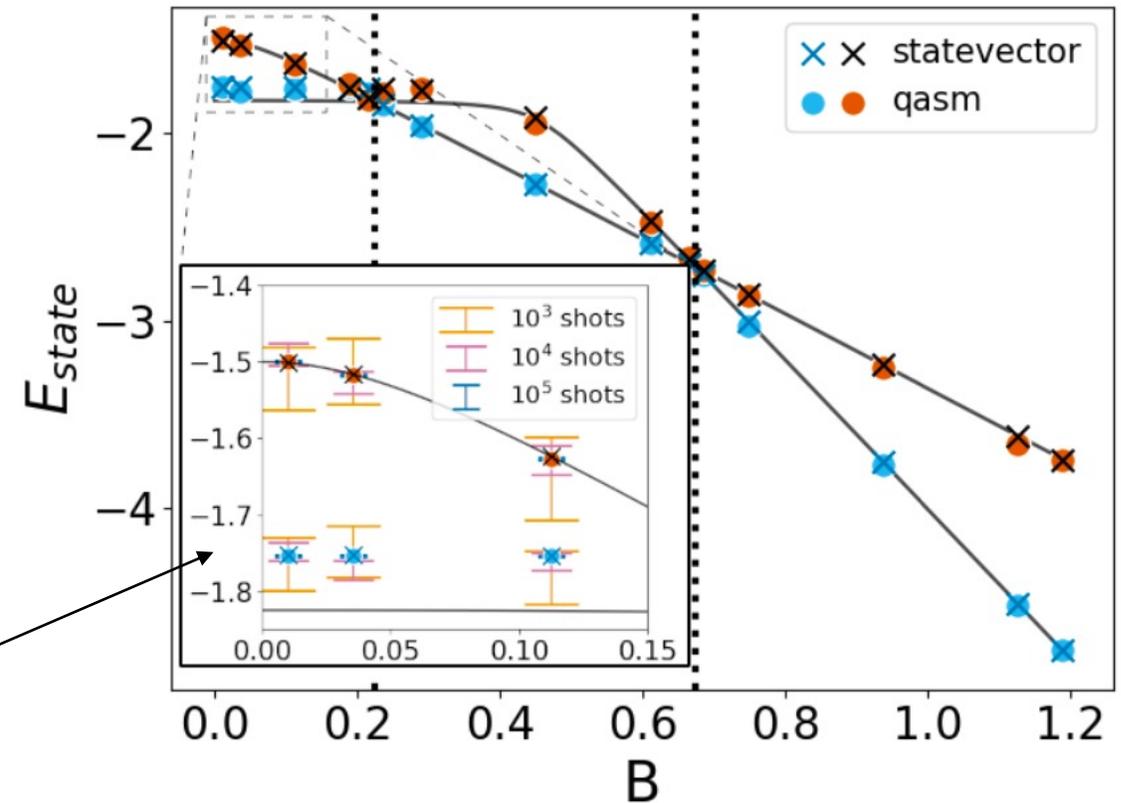
$$H' = H + \beta_0 |\psi_{GS}\rangle \langle \psi_{GS}|.$$

### Hardware efficient ansatz



Energy of the gs and 1st es for N=5,  $\gamma = 0.81$ .

Shot noise effect



Grossi, Kiss et al, Finite-size criticality in fully connected spin models on superconducting quantum hardware - PhysRevE.107.024113

# Runs on real hardware (IBMQ)

Blue: raw (starting from classical optimized parameters with fine tuning on noise).  
Red: calibrated with inverse of the error matrices and zero noise extrapolation with exponential fit.

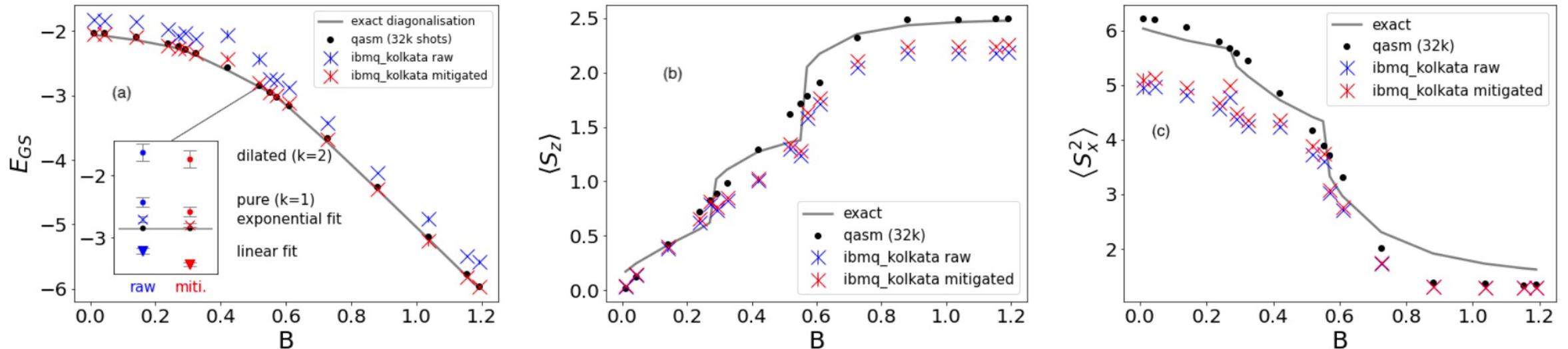
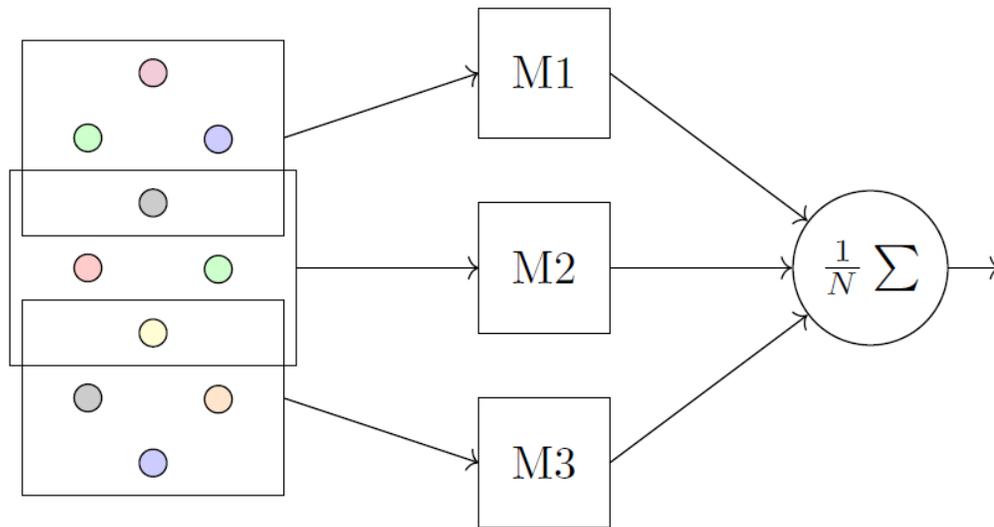


Figure 7. Ground state energy (GS) (a), and magnetization  $\langle S_x^2 \rangle$  (b), and  $\langle S_z \rangle$  (c), for  $N = 5$  spins at  $\gamma = 0.49$  values. Points are obtained on the superconducting device `ibmq_kolkata` with (red) and without (blue) error mitigation compared to noiseless simulation (black) and exact values (line). The inset shows the extrapolation to the zero noise regime, both with an exponential and linear fit.

Grossi, Kiss et al, *Finite-size criticality in fully connected spin models on superconducting quantum hardware* - *PhysRevE.107.024113*

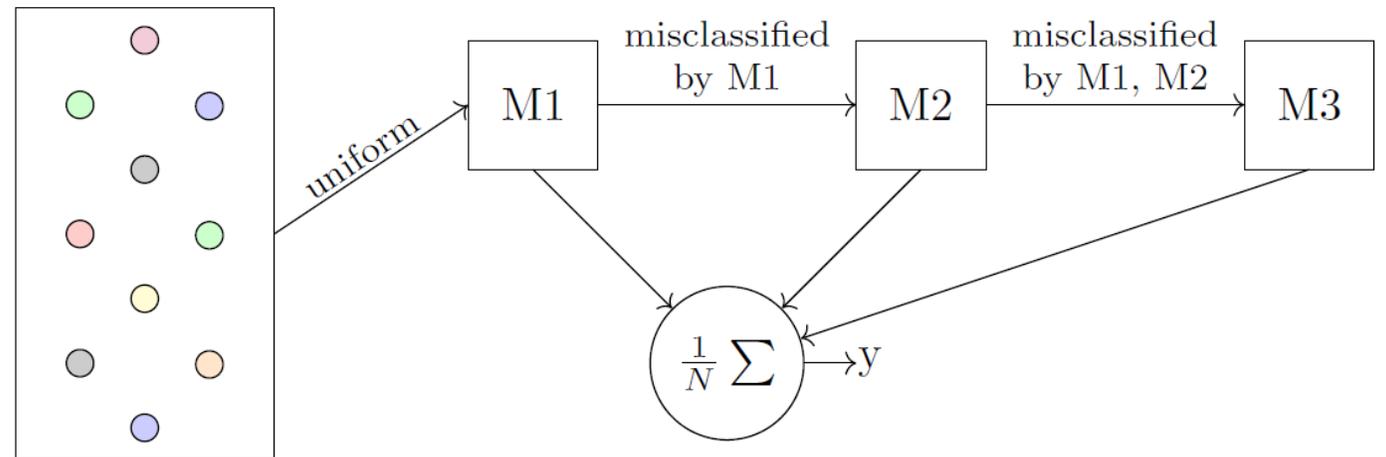
# Ensemble Techniques

- Evaluate ensemble schemes (**BAGGING** and **BOOSTING**) into *quantum neural networks (QNN)*
- *Layer-wise analysis of quantum neural network performance in the ensemble setting*
- Investigate the potential advantages of bagging techniques in mitigating the effects of noise



## BAGGING

- any instance of QNN is trained on a bootstrapped subset of the data  
- analogy with **quantum circuit splitting** / divide-and-conquer techniques (e.g. Lowe et al. 22, Yoshikawa et al. 22))



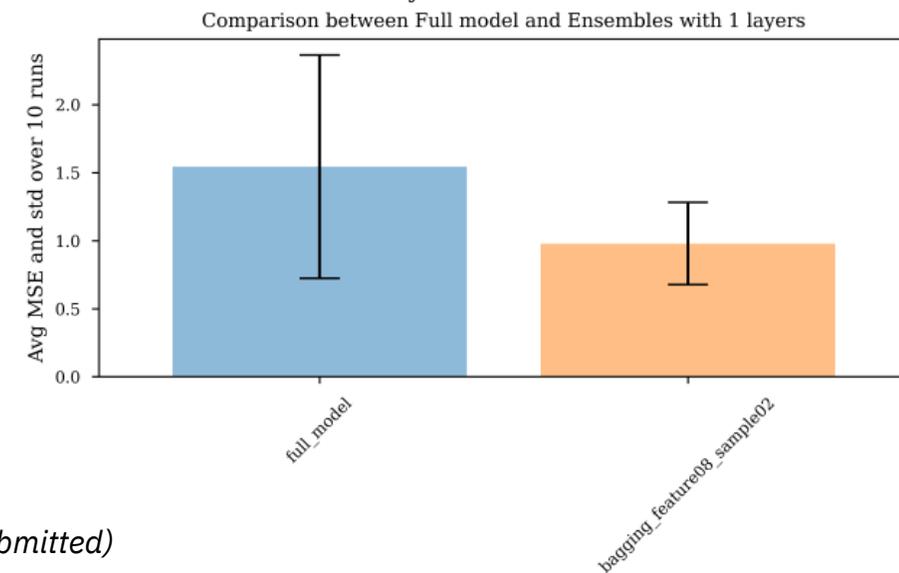
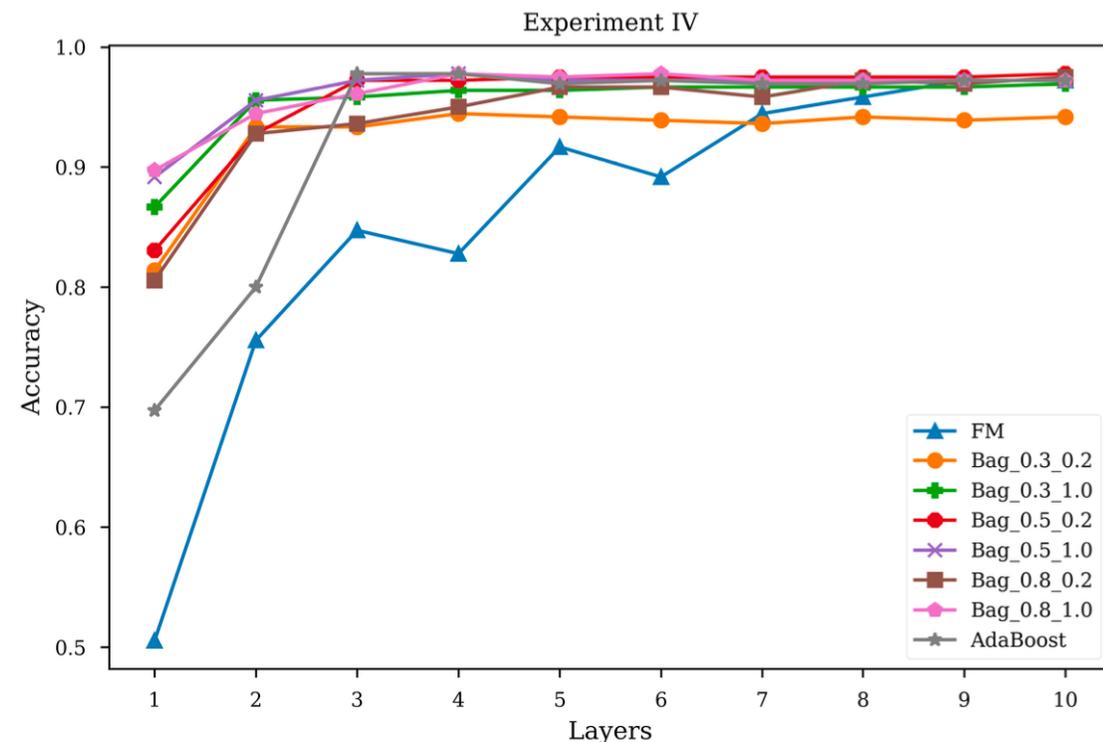
## BOOSTING

*training a sequence of predictors*

Includini, Grossi, Vallecorsa et al – Resource Saving via Ensemble Techniques for Quantum Neural Networks (Submitted)

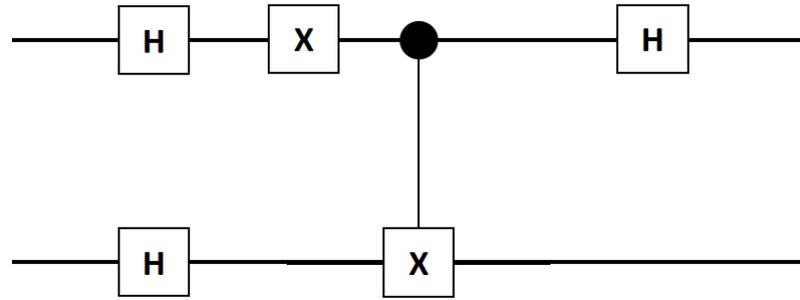
# Ensemble: Settings & Results

- Tested the **LINEAR DATASET** on the IBM Lagos QPU (7 qubits)
- Ensemble technique: **BAGGING**  
80% features 20% samples
- **-1/3** of the MSE on average

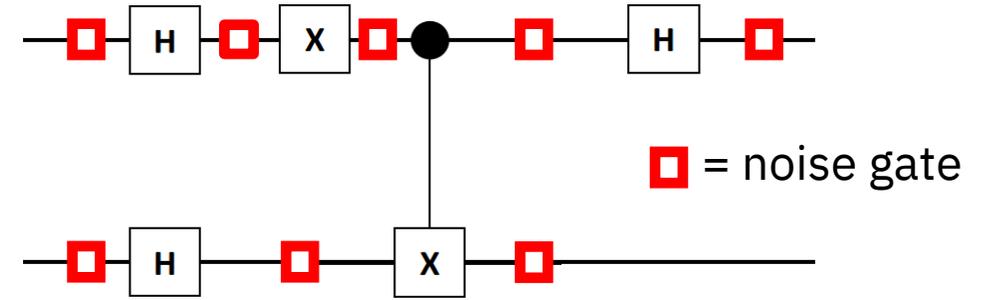


Includini, Grossi, Vallecorsa et al – Resource Saving via Ensemble Techniques for Quantum Neural Networks (Submitted)

# Noise Models



Noises (like gates) formally act instantly: Lindblad  
→ Kraus  $\rho \rightarrow \sum_i K_i \rho K_i^\dagger$   $\sum_i K_i^\dagger K_i = 1$



*Standard noise simulation (e.g. in Qiskit)*

- Gates and noise are formally **decoupled** (a sort of Trotterization), because time scales are small (IBM: gate time  $\sim 10^{-8}$  s, decoherence times  $\sim 10^{-4}$  s)
- Use the **quantum-jump-like approach** to replace the density matrix with (stochastic) state vector → stochastic (unravelling) dynamics



Di Bartolomeo, Vischi, Wixinger, Grossi et al., A novel approach to noisy gates for simulating quantum computers - <https://arxiv.org/abs/2301.04173>

# Comparison of the algorithms

SEE QTI lectures:

<https://indico.cern.ch/event/1247873/>

Kraus map for density matrix  $\mathcal{E}(\rho) = \sum_i K_i \rho K_i^\dagger, \quad \sum_i K_i^\dagger K_i = \mathbb{1}.$

Unravelling for the state vector  $|\psi'\rangle = \frac{1}{\sqrt{p_j}} K_j |\psi\rangle, \quad p_j = |\langle \psi | K_j^\dagger K_j | \psi \rangle|^2.$

State vector simulations with standard method

Vischi, Wixinger, Grossi et al., A novel approach to noisy gates for simulating quantum computers - <https://arxiv.org/abs/2301.04173>

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## Algorithm 1 QISKIT SIMULATION

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**Input:** Initial state  $|\psi_0\rangle$ , a noiseless circuit  $C = \{U^{(1)}, \dots, U^{(n_g)}\}$  composed by  $n_g$  gates  $U^{(i)}$  and number of samples  $N_s$

**for**  $0 \leq k \leq N_s$  **do**

**while**  $1 \leq i \leq n_g$  **do**

        compute  $|\psi_k\rangle^{(i)} = U^{(i)} |\psi_k\rangle^{(i-1)}$

        compute  $p_j = |\langle \psi_k |^{(i)} K_j^\dagger K_j | \psi_k \rangle^{(i)}|^2$

        sample  $K_j$  operator from  $\{p_j\}$

        update the state to  $|\psi_k\rangle^{(i)} = \frac{1}{\sqrt{p_j}} K_j |\psi_k\rangle^{(i)}$

**end**

    compute  $\rho_k = |\psi_k\rangle^{(n_g)} \langle \psi_k |^{(n_g)}$

**end**

**Output:**  $\rho_f = \frac{1}{N_s} \sum_{k=1}^{N_s} \rho_k$

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## Algorithm 2 NOISY GATES SIMULATION

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**Input:** Initial state  $|\psi_0\rangle$ , a noiseless circuit  $C = \{U^{(1)}, \dots, U^{(n_g)}\}$  composed by  $n_g$  gates  $U^{(i)}$  and number of samples  $N_s$

**for**  $0 \leq k \leq N_s$  **do**

    map a noisy circuit  $\tilde{C} = \{N^{(1)}, \dots, N^{(n_g)}\}$  on  $C$

    sample stochastic processes  $\xi$  inside noisy gates  $N^{(i)}$

    compute  $|\psi_k\rangle = N^{(n_g)} \dots N^{(1)} |\psi_0\rangle$

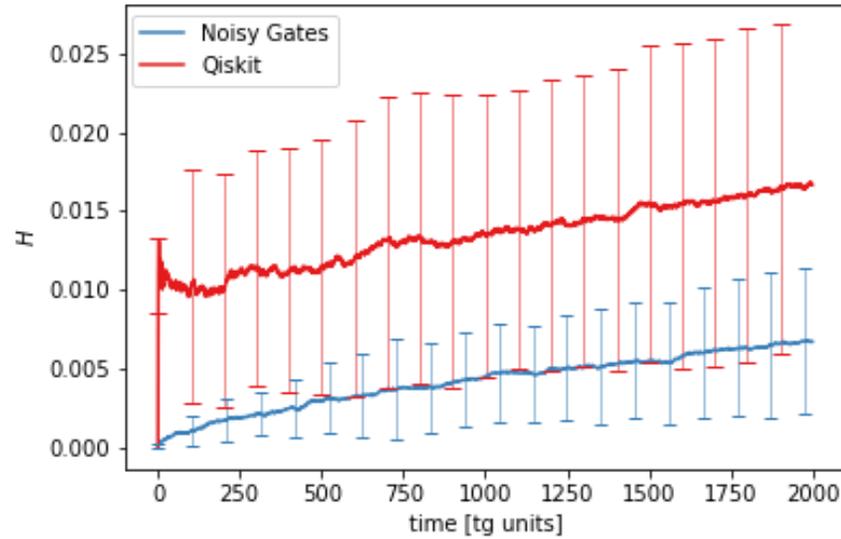
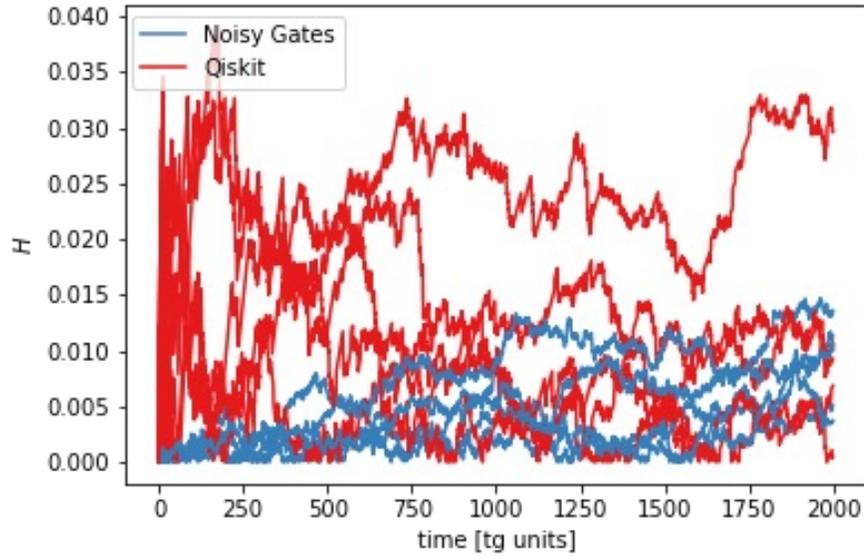
    compute  $\rho_k = |\psi_k\rangle \langle \psi_k |$

**end**

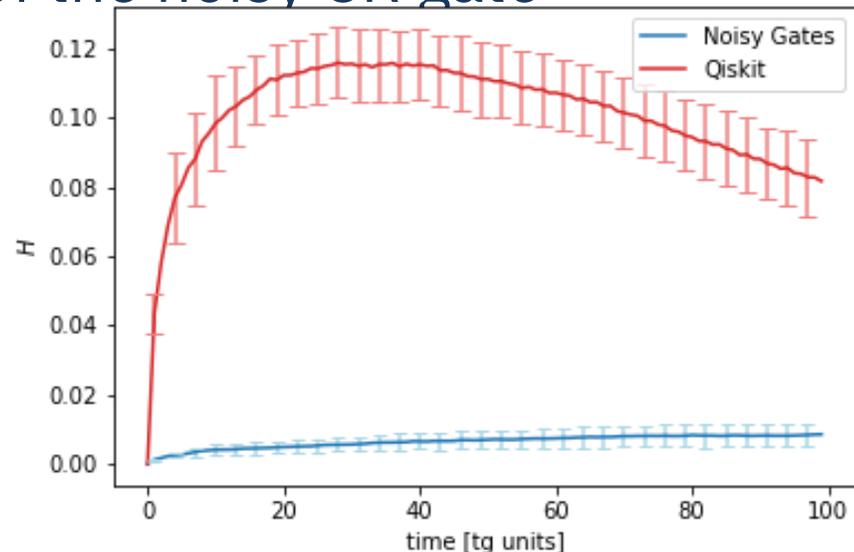
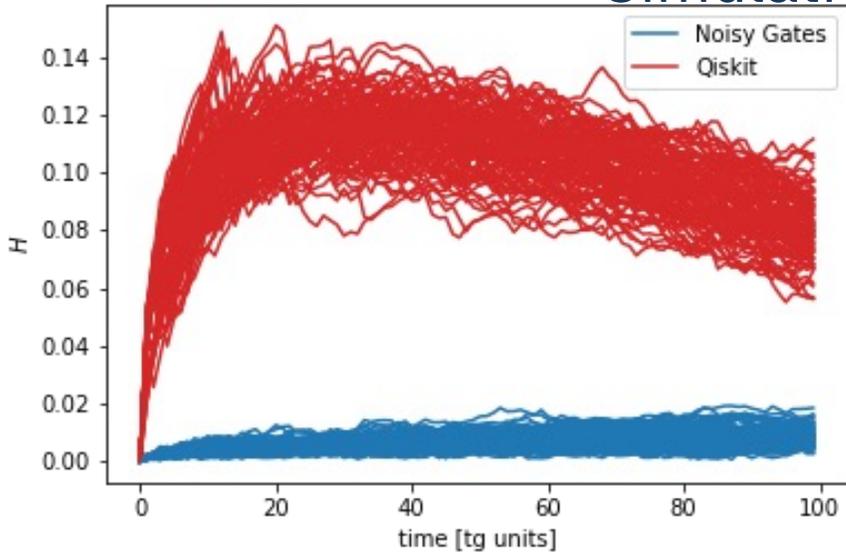
**Output:**  $\rho_f = \frac{1}{N_s} \sum_{k=1}^{N_s} \rho_k$

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# Simulation of the noisy X gate



# Simulation of the noisy CR gate



## Hellinger Distance

Lindblad and noisy gates

Lindblad and Qiskit simulator

$$H(P, Q) = \frac{1}{\sqrt{2}} \sqrt{\sum_{i=1}^n (\sqrt{p_i} - \sqrt{q_i})^2}$$

Di Bartolomeo, Vischi, Wixinger, Grossi et al., A novel approach to noisy gates for simulating quantum computers - <https://arxiv.org/abs/2301.04173>



# quantum-gates 1.0.2

✓
[Latest version](#)

```
pip install quantum-gates
```

❏

Released: Feb 2, 2023

Quantum Noisy Gates Simulation with Python

## Navigation

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## Project description

### Noisy Quantum Gates

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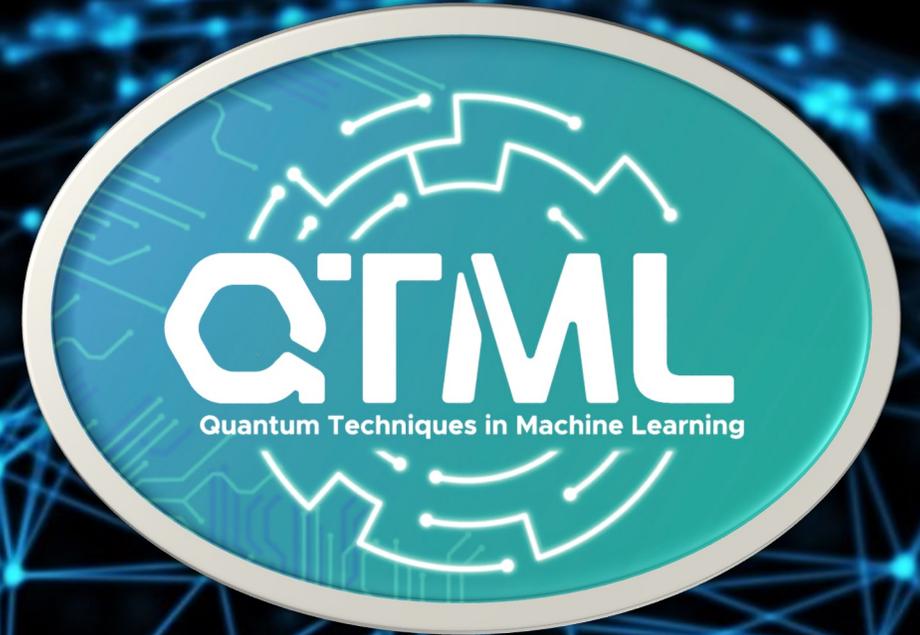
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Implementation of the Noisy Quantum Gates model, which is soon to be published. It is a novel method to simulate the noisy behaviour of quantum devices by incorporating the noise directly in the gates, which become stochastic matrices.



# CERN 20-24 November 2023

Annual international conference focusing on the interdisciplinary field of quantum technology and machine learning



M.Grossi - QTI - 2023 openlab Technical Workshop

The background is a dark blue gradient with several glowing blue lines and a network of nodes. The nodes are small blue dots connected by thin blue lines, forming a complex web-like structure. The lines are curved and intersect, creating a sense of depth and movement.

**CERN QTI**

**<https://quantum.cern/>**



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